

Water flows with the velocity $U_\infty = 0.2 \text{ m/s}$ parallel to a plane wall. The following calculations refer to the position $x = 6 \text{ m}$ measured downstream from the leading edge. The water properties can be evaluated at 20°C .

(a) A probe is to be inserted in the viscous sublayer to the position represented by $y^+ = 2.7$. Calculate the actual spacing y (mm) between the probe and the wall.

(b) Calculate the boundary layer thickness δ , assuming that the length x is covered by turbulent boundary layer flow.

(c) Calculate the heat transfer coefficient averaged over the length x .

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In[*]:= U∞ = 0.2; L = 6;
ρ = ThermodynamicData["Water", "Density",
  {"Temperature" → Quantity[20, "DegreesCelsius"]}] [[1]];
μ = ThermodynamicData["Water", "Viscosity",
  {"Temperature" → Quantity[20, "DegreesCelsius"]}] [[1]];
κ = ThermodynamicData["Water", "Density",
  {"Temperature" → Quantity[20, "DegreesCelsius"]}] [[1]];
Cp = ThermodynamicData["Water", "IsobaricHeatCapacity",
  {"Temperature" → Quantity[20, "DegreesCelsius"]}] [[1]];
ν =  $\frac{\mu}{\rho}$ ; Pr =  $\frac{\mu C_p}{\kappa}$ ;
ReL =  $\frac{U_\infty L}{\nu}$ 
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Out[*]= 1.19594 × 106
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In[*]:= Rex =  $\frac{U_\infty x}{\nu}$ ;
Cf =  $\frac{0.0624}{Re_x^{1/5}}$ ;
uτ =  $U_\infty \sqrt{\left(\frac{C_f}{2}\right)}$ ;
y+ =  $\frac{y u_\tau}{\nu}$ ;
Solve[(y+ == 2.7) /. x → L, y, Reals]
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Out[*]= {{y → 0.000310813}}
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In[*]:= δ = 0.4013 x Rex-1/5 /. x → L
Out[*]= 0.146581
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In[*]:= Nux =  $\frac{C_f}{2} Re_x Pr^{1/3}$ ;
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In[*]:= NuMean =  $\int_0^L \frac{Nu_x}{x} dx$ 
Out[*]= 458.059
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In[*]:= hMean = NuMean  $\frac{x}{L}$   
Out[*]= 76206.3
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